

Unsupervised Domain Adaptation via Structurally Regularized Deep Clustering

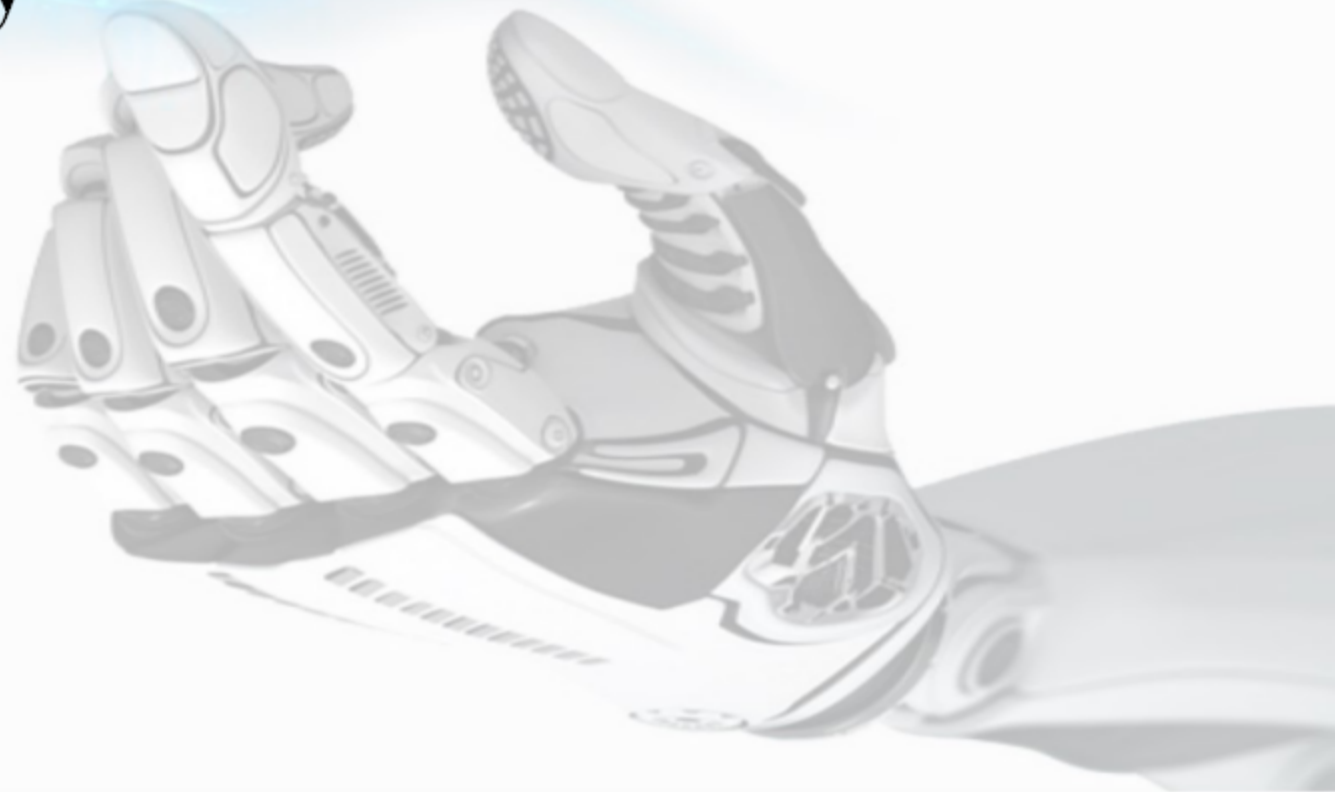
Authors: Hui Tang, Ke Chen, Kui Jia



Institution: South China University of Technology

CONTENTS

- 1. Problem Definition**
- 2. Our Uncovering Strategy**
- 3. Experiments**
- 4. Future directions**



PROBLEM DEFINITION

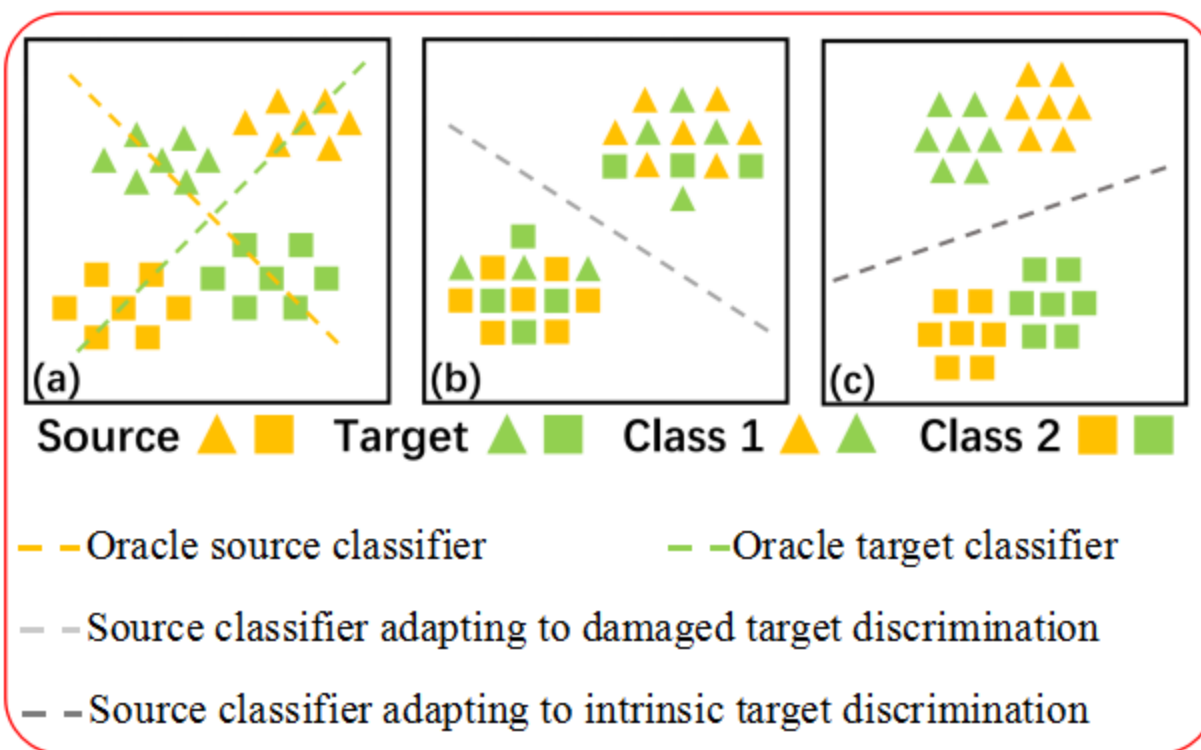
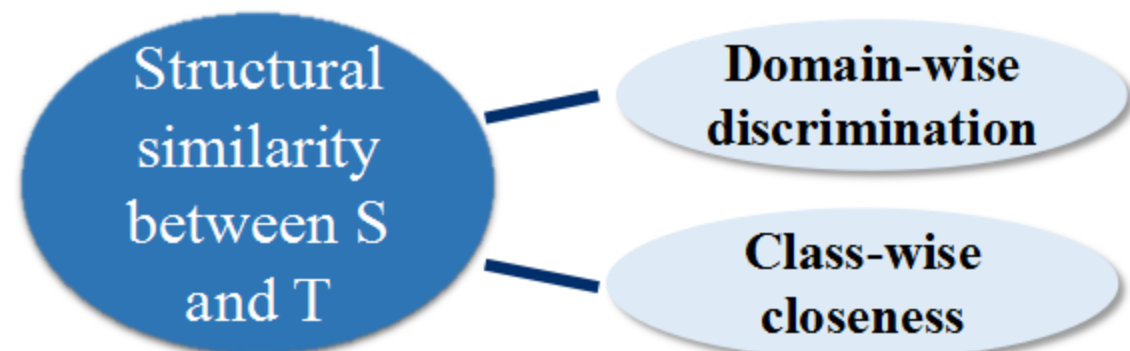
- Source domain $\mathcal{S} = \{(x_j^s, y_j^s)\}_{j=1}^{n_s}$
 - Target domain $\mathcal{T} = \{x_i^t\}_{i=1}^{n_t}$
 - Feature embedding function $\varphi(\cdot; \theta) : \mathcal{X} \rightarrow \mathcal{Z}$ lifts any $x \in \mathcal{X}$ to the feature space \mathcal{Z} , i.e. $z = \varphi(x)$.
 - Classifier $f(\cdot; \mathcal{G}) : \mathcal{Z} \rightarrow R^K$ with softmax at the top outputs a probability vector $p = \text{softmax}(f(z))$.
- A shared label space \mathcal{Y} : $y^s, y^t \in \{1, 2, \dots, K\}$.

➤ **Objective:** Given labeled data on \mathcal{S} , UDA is to predict class labels for unlabeled data sampled from \mathcal{T} by learning $\varphi(\cdot)$ and $f(\cdot)$ on both $\{(x_j^s, y_j^s)\}_{j=1}^{n_s}$ and $\{x_i^t\}_{i=1}^{n_t}$.

- Transductive UDA is to measure performance of the learned $\varphi(\cdot)$ and $f(\cdot)$ on $\{x_i^t\}_{i=1}^{n_t}$.
- Inductive UDA is to evaluate on **held-out** instances sampled from the same \mathcal{T} .
- This subtle difference is in fact important since **off-the-shelf** models are expected.

OUR UNCOVERING STRATEGY

- Assumption of structural domain similarity (a):



- Existing transferring strategy of learning aligned features across domains (b) \longrightarrow a sub-optimal generalization.

- Based on the assumption, our strategy of uncovering intrinsic discrimination of target data (c) \longrightarrow an adapted classifier closer to oracle target classifier.

OUR UNCOVERING STRATEGY

- **Motivation:** Mainstream UDA methods take the transferring strategy, which has a potential risk of damaging the intrinsic discrimination of target data, as discussed in [2, 3, 4].
- **Solution:** We directly uncover the intrinsic target discrimination via discriminative clustering of target data and constrain the clustering solutions using structural source regularization that hinges on our assumed structural domain similarity.

[2] Xinyang Chen, Sinan Wang, Mingsheng Long, et al. Transferability vs. discriminability: Batch spectral penalization for adversarial domain adaptation. ICML2019.

[3] Yuan Shi and Fei Sha. Information-theoretical learning of discriminative clusters for unsupervised domain adaptation. ICML2012.

[4] Han Zhao, Remi Tachet Des Combes, Kun Zhang, et al. On learning invariant representations for domain adaptation. ICML2019.

OUR UNCOVERING STRATEGY

- **Structurally Regularized Deep Clustering (SRDC)** *implicitly* achieves feature alignment between the two domains.

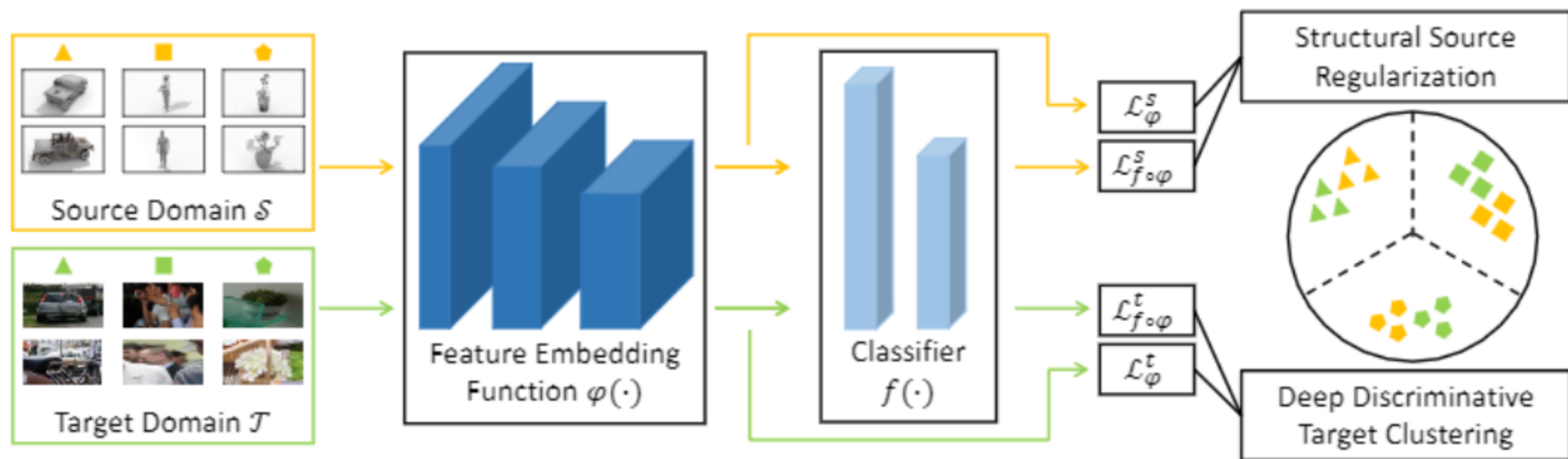


Figure 1. (Best viewed in color). Pipeline of our proposed method. The colors of orange and green denote different domains. The shapes of triangle, rectangle, and pentagon denote different classes. Based on the assumed structural similarity across domains, our losses of $\mathcal{L}_{f \circ \varphi}^t$ and \mathcal{L}_{φ}^t uncover the intrinsic discrimination of unlabeled target data and those of $\mathcal{L}_{f \circ \varphi}^s$ and \mathcal{L}_{φ}^s transfer the global, discriminative structure of labeled source data via joint training. An example of the effect of our proposed method is shown in the circle.

OUR UNCOVERING STRATEGY

- **Deep discriminative target clustering** [5] minimizes the KL divergence between predictive label distribution of the network and an introduced auxiliary one:

$$\min_{Q^t, \{\theta, \vartheta\}} \mathcal{L}_{f \circ \varphi}^t = \text{KL}(Q^t \| P^t) + \sum_{k=1}^K \varrho_k^t \log \varrho_k^t, \quad (1)$$

We collectively write $\{p_i^t\}_{i=1}^{n_t}$ as P^t .

Q^t is the introduced auxiliary counterpart.

$\rho_k^t = 1/n_t \sum_{i=1}^{n_t} q_{i,k}^t$ is the predicted target label distribution.

- Optimization takes **alternating** steps:

Auxiliary distribution update

$$q_{i,k}^t = \frac{p_{i,k}^t / (\sum_{i'=1}^{n_t} p_{i',k}^t)^{\frac{1}{2}}}{\sum_{k'=1}^K p_{i,k'}^t / (\sum_{i'=1}^{n_t} p_{i',k'}^t)^{\frac{1}{2}}}. \quad (2)$$



Network update

$$\min_{\theta, \vartheta} -\frac{1}{n_t} \sum_{i=1}^{n_t} \sum_{k=1}^K q_{i,k}^t \log p_{i,k}^t. \quad (3)$$

- We also enhance target discrimination with **deep embedding clustering** in the feature space [6]:

$$\tilde{p}_{i,k}^t = \frac{\exp((1 + \|z_i^t - \mu_k\|^2)^{-1})}{\sum_{k'=1}^K \exp((1 + \|z_i^t - \mu_{k'}\|^2)^{-1})}. \quad (4)$$

where μ_k is the learnable cluster center and $\tilde{p}_{i,k}^t$ is a probability vector of soft cluster assignment.

$$\min_{\tilde{Q}^t, \theta, \{\mu_k^t\}_{k=1}^K} \mathcal{L}_{\varphi}^t = \text{KL}(\tilde{Q}^t \| \tilde{P}^t) + \sum_{k=1}^K \tilde{\varrho}_k^t \log \tilde{\varrho}_k^t, \quad (5)$$

OUR UNCOVERING STRATEGY

- **Structural source regularization:** Replacing the auxiliary distribution with that formed by ground-truth labels of source data implements the structural source regularization via a simple strategy of joint network training:

$$\min_{\theta, \vartheta} \mathcal{L}_{f \circ \varphi}^s = -\frac{1}{n_s} \sum_{j=1}^{n_s} \sum_{k=1}^K \mathbb{I}[k = y_j^s] \log p_{j,k}^s, \quad (7)$$

$$\min_{\theta, \{\mu_k\}_{k=1}^K} \mathcal{L}_{\varphi}^s = -\frac{1}{n_s} \sum_{j=1}^{n_s} \sum_{k=1}^K \mathbb{I}[k = y_j^s] \log \tilde{p}_{j,k}^s, \quad (8)$$

where

$$\tilde{p}_{j,k}^s = \frac{\exp((1 + \|z_j^s - \mu_k\|^2)^{-1})}{\sum_{k'=1}^K \exp((1 + \|z_j^s - \mu_{k'}\|^2)^{-1})}. \quad (9)$$

- We also enhance structural regularization with **soft selection of less divergent source examples:**

$$w^s(x^s) = \frac{1}{2} \left(1 + \frac{c_{y^s}^{t\top} x^s}{\|c_{y^s}^t\| \|x^s\|} \right) \in [0, 1]. \quad (12)$$

where $\{c_k^t\}_{k=1}^K$ are the K target cluster centers in the feature space.

$$\mathcal{L}_{f \circ \varphi}^s(\cdot; \{w_j^s\}_{j=1}^{n_s}) = -\frac{1}{n_s} \sum_{j=1}^{n_s} w_j^s \sum_{k=1}^K \mathbb{I}[k = y_j^s] \log p_{j,k}^s, \quad (13)$$

$$\mathcal{L}_{\varphi}^s(\cdot; \{w_j^s\}_{j=1}^{n_s}) = -\frac{1}{n_s} \sum_{j=1}^{n_s} w_j^s \sum_{k=1}^K \mathbb{I}[k = y_j^s] \log \tilde{p}_{j,k}^s. \quad (14)$$

OUR UNCOVERING STRATEGY

■ Training algorithm

Algorithm 1 Training algorithm for SRDC, E denotes the training epoch, I denotes the training iteration, B_t and B_s denote the mini-batches.

Input: unlabeled target samples $\mathcal{T} = \{x_i^t\}_{i=1}^{n_t}$; labeled source samples $\mathcal{S} = \{(x_j^s, y_j^s)\}_{j=1}^{n_s}$

Output: $\theta, \vartheta, \{\mu_k\}_{k=1}^K$

- 1: Initialize: $\theta, \vartheta, \{\mu_k\}_{k=1}^K, q_{i,k}^t = \tilde{q}_{i,k}^t = \mathbb{I}[k = \hat{y}_i^t]$ for $i \in \{1, 2, \dots, n_t\}$ and $k \in \{1, 2, \dots, K\}, w_j^s = 1$ for $j \in \{1, 2, \dots, n_s\}, E = 1$
- 2: **while** not converge **do**
- 3: **for** $I \leftarrow 1, MAX_ITER$ **do**
- 4: Sample B_t and B_s from \mathcal{T} and \mathcal{S}
- 5: **if** $E \neq 1$ **then**
- 6: Compute $q_{i,k}^t$ and $\tilde{q}_{i,k}^t$ by using (2)
- 7: **end if**
- 8: Update $\theta, \vartheta, \{\mu_k\}_{k=1}^K$ by minimizing (11) on B_t and B_s
- 9: **end for**
- 10: Compute $\{c_k^t\}_{k=1}^K$ by standard K -means clustering
- 11: Compute $w_j^s = 1, j \in \{1, 2, \dots, n_s\}$ by using (12)
- 12: Initialize: $\{\mu_k\}_{k=1}^K$
- 13: $E = E + 1$
- 14: **end while**

EXPERIMENTS

■ Ablation study:

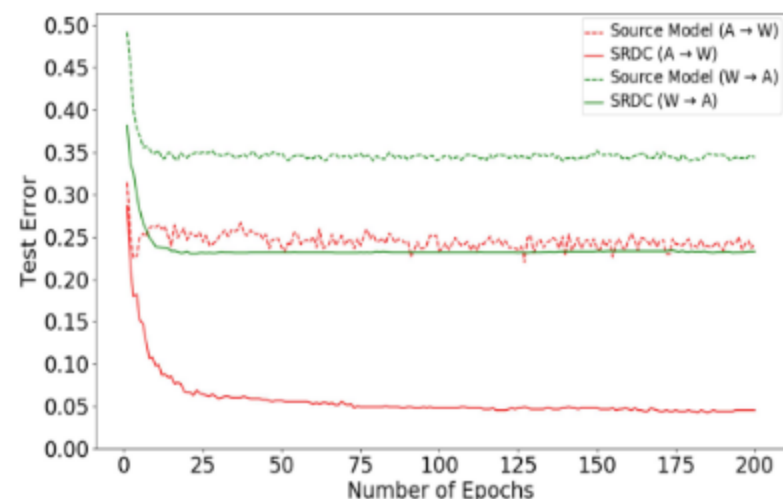
Method	A \rightarrow W	A \rightarrow D	D \rightarrow A	W \rightarrow A	Avg
Source Model	77.8 \pm 0.2	82.1 \pm 0.2	64.5 \pm 0.2	66.1 \pm 0.2	72.6
SRDC (w/o structural source regularization)	87.3 \pm 0.0	92.1 \pm 0.1	73.9 \pm 0.1	75.0 \pm 0.1	82.1
SRDC (w/o feature discrimination)	94.2 \pm 0.4	94.3 \pm 0.4	74.3 \pm 0.2	75.5 \pm 0.4	84.6
SRDC (w/o soft source sample selection)	94.8 \pm 0.2	94.6 \pm 0.3	74.6 \pm 0.3	75.7 \pm 0.3	84.9
SRDC	95.7\pm0.2	95.8\pm0.2	76.7\pm0.3	77.1\pm0.1	86.3

Each component is important!

■ Comparative experiments under inductive UDA setting:

Method	A \rightarrow W	A \rightarrow D	D \rightarrow A	W \rightarrow A	Avg
Source Model	79.3	81.6	63.1	65.7	72.4
DANN [16]	80.8	82.4	66.0	64.6	73.5
MCD [48]	86.5	86.7	72.4	70.9	79.1
SRDC	91.9	91.6	75.6	75.7	83.7
Oracle Model	98.8	97.6	87.8	87.8	93.0

■ Convergence performance



Better and more stable!

Figure 5. Convergence.

Much closer to Oracle Model! Stronger generalization ability!

EXPERIMENTS

■ Source refinement



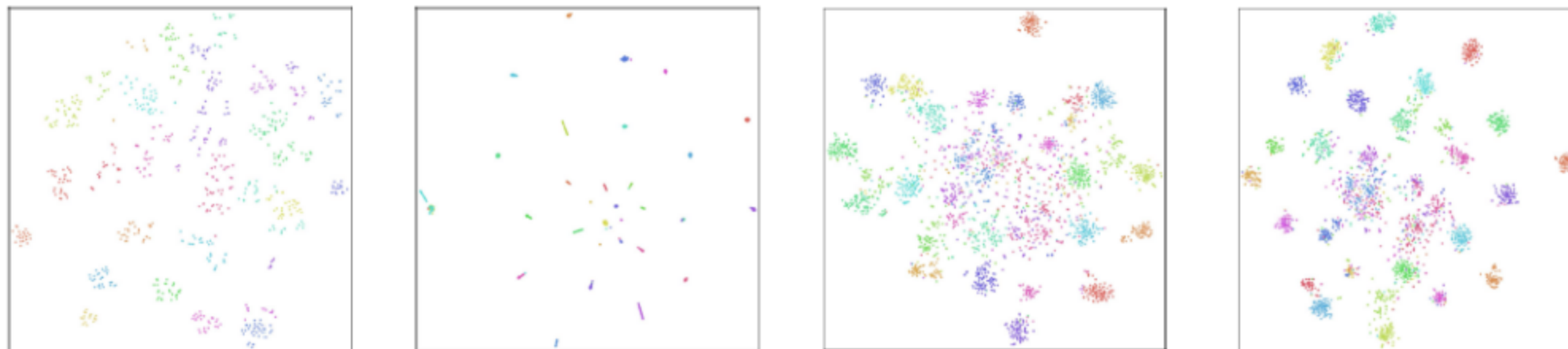
From canonical viewpoint

From canonical, top-down, bottom-up, and side viewpoints

Figure 2. The images on the left are randomly sampled from the target domain A and those on the right are the top-ranked (the 3rd column) and bottom-ranked (the 4th column) samples from the source domain W for three classes. Note that the red numbers are the source weights computed by (12).

EXPERIMENTS

■ Visualization by t-SNE and confusion matrix



(a) Source Model: $A \rightarrow W$

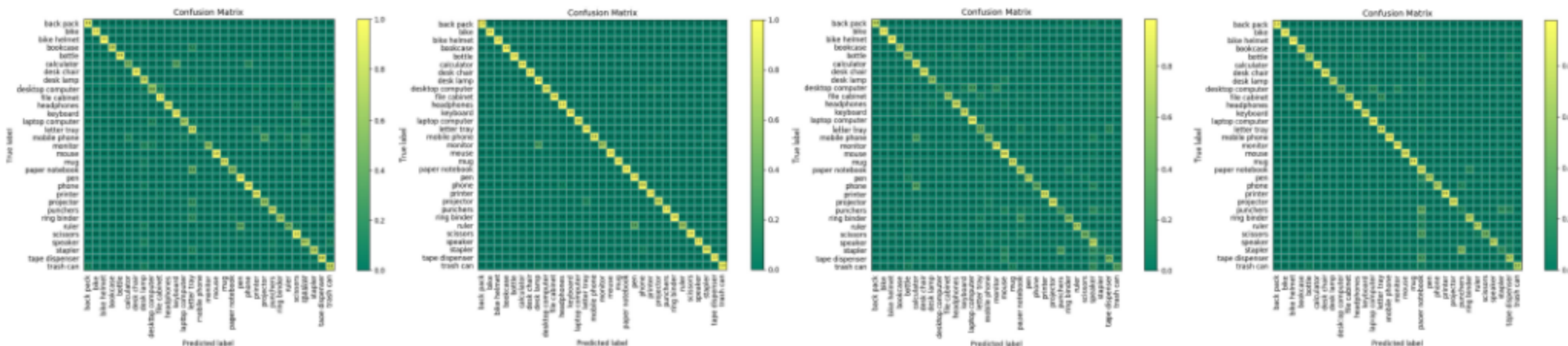
(b) SRDC: $A \rightarrow W$

(c) Source Model: $W \rightarrow A$

(d) SRDC: $W \rightarrow A$

Figure 3. The t-SNE visualization of embedded features on the target domain. Note that different classes are denoted by different colors.

Significant improvement!



(a) Source Model: $A \rightarrow W$

(b) SRDC: $A \rightarrow W$

(c) Source Model: $W \rightarrow A$

(d) SRDC: $W \rightarrow A$

Figure 4. The confusion matrix on the target domain. (Zoom in to see the exact class names!)

EXPERIMENTS

Comparison with SOTA

Method	A \rightarrow W	D \rightarrow W	W \rightarrow D	A \rightarrow D	D \rightarrow A	W \rightarrow A	Avg
Source Model [21]	77.8 \pm 0.2	96.9 \pm 0.1	99.3 \pm 0.1	82.1 \pm 0.2	64.5 \pm 0.2	66.1 \pm 0.2	81.1
MDD [66]	94.5 \pm 0.3	98.4 \pm 0.1	100.0 \pm 0.0	93.5 \pm 0.2	74.6 \pm 0.3	72.2 \pm 0.1	88.9
CAN [27]	94.5 \pm 0.3	99.1 \pm 0.2	99.8 \pm 0.2	95.0 \pm 0.3	78.0 \pm 0.3	77.0 \pm 0.3	90.6
SRDC	95.7 \pm 0.2	99.2 \pm 0.1	100.0 \pm 0.0	95.8 \pm 0.2	76.7 \pm 0.3	77.1 \pm 0.1	90.8

Table 3. Results (%) on Office-31 (ResNet-50).

Methods	I \rightarrow P	P \rightarrow I	I \rightarrow C	C \rightarrow I	C \rightarrow P	P \rightarrow C	Avg
Source Model [21]	74.8 \pm 0.3	83.9 \pm 0.1	91.5 \pm 0.3	78.0 \pm 0.2	65.5 \pm 0.3	91.2 \pm 0.3	80.7
SAFN+ENT [60]	79.3 \pm 0.1	93.3 \pm 0.4	96.3 \pm 0.4	91.7 \pm 0.0	77.6 \pm 0.1	95.3 \pm 0.1	88.9
SymNets [68]	80.2 \pm 0.3	93.6 \pm 0.2	97.0 \pm 0.3	93.4 \pm 0.3	78.7 \pm 0.3	96.4 \pm 0.1	89.9
SRDC	80.8 \pm 0.3	94.7 \pm 0.2	97.8 \pm 0.2	94.1 \pm 0.2	80.0 \pm 0.3	97.7 \pm 0.1	90.9

Table 4. Results (%) on ImageCLEF-DA (ResNet-50).

Methods	Ar \rightarrow Cl	Ar \rightarrow Pr	Ar \rightarrow Rw	Cl \rightarrow Ar	Cl \rightarrow Pr	Cl \rightarrow Rw	Pr \rightarrow Ar	Pr \rightarrow Cl	Pr \rightarrow Rw	Rw \rightarrow Ar	Rw \rightarrow Cl	Rw \rightarrow Pr	Avg
Source Model [21]	34.9	50.0	58.0	37.4	41.9	46.2	38.5	31.2	60.4	53.9	41.2	59.9	46.1
SymNets [68]	47.7	72.9	78.5	64.2	71.3	74.2	64.2	48.8	79.5	74.5	52.6	82.7	67.6
MDD [66]	54.9	73.7	77.8	60.0	71.4	71.8	61.2	53.6	78.1	72.5	60.2	82.3	68.1
SRDC	52.3	76.3	81.0	69.5	76.2	78.0	68.7	53.8	81.7	76.3	57.1	85.0	71.3

Table 5. Results (%) on Office-Home (ResNet-50).

Outperform SOTA!



Code

FUTURE DIRECTIONS

- To investigate more effective clustering methods for target discrimination.
- To discover more helpful manners to enforce structural source regularization.
- To explore novel UDA paradigms with theoretical guidance, which can preserve the intrinsic target discrimination as much as possible.



Thanks for listening !